

**Quiz 4 - Math 374, Frank Thorne (thorne@math.sc.edu)**

**Friday, September 22, 2017**

- (1) Prove: The sum of an even integer and an odd integer is odd.

**Proof.** Suppose that  $x$  is an even integer and that  $y$  is an odd integer. Then, there are integers  $m$  and  $n$  for which  $x = 2m$  and  $y = 2n + 1$ . Thus,  $x + y = 2m + 2n + 1 = 2(m + n) + 1$ . Since we have written  $x + y$  as twice an integer plus 1, it is odd, as desired.